

Midterm #1

FRI, 2/26

exam: 8⁰⁰-8⁵⁵ AM

upload work by 9³⁰ AM
PDF

format

- check it out! link in email
- show-your-work problems ~ 2
- short answer problems ~ 10
no "real" work needed

practice

- review HW
- practice problems + solutions

tools

- calculators allowed but: show work
- notes allowed but: watch time

Questions?

- Lots of review

Gaussian elimination, null spaces,
determinants, eigenstuff, ...

not on
exam

- LU decomposition
- diagonalization

THEME: orthogonality

- fundamental theorem
 $\text{col}(A)$ and $\text{null}(A^T)$ are orthogonal complements
- consistency of linear systems
- least squares solutions
application: least squares lines (linear regression)
application: data fitting
- orthogonal projections
projection matrices
using orthogonal bases
- Gram-Schmidt + QR
- orthogonal matrices
- diagonalizability
- spectral theorem

EG $A \rightsquigarrow \text{RREF } B$

$$\text{null}(A) = \text{null}(B)$$

solutions to $Ax=0$

$$B = \begin{bmatrix} \textcircled{1} & 4 & 0 & 7 & 0 \\ 0 & 0 & \textcircled{1} & -2 & 0 \\ 0 & 0 & 0 & 0 & \textcircled{1} \end{bmatrix}$$

$\underbrace{\quad}_{x_2 \text{ free}} \quad \underbrace{\quad}_{x_4 \text{ free}}$

$$\textcircled{x_1} + 4x_2 + 7x_4 = 0$$

$$\textcircled{x_3} - 2x_4 = 0$$

$$\textcircled{x_5} = 0$$

general solution to $Ax=0$
 $Bx=0$:

$$\begin{bmatrix} -4x_2 - 7x_4 \\ x_2 \\ 2x_4 \\ x_4 \\ 0 \end{bmatrix} = x_2 \begin{bmatrix} -4 \\ 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} + x_4 \begin{bmatrix} -7 \\ 0 \\ 2 \\ 1 \\ 0 \end{bmatrix}$$

basis for $\text{null}(A)$