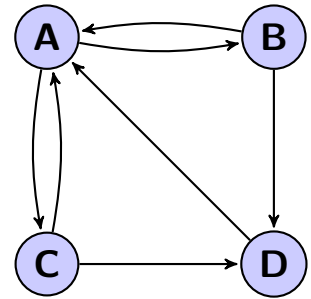


Problem 6. Suppose the internet consists of only the four webpages A, B, C, D which link to each other as indicated in the diagram.



Rank these webpages by computing their PageRank vector.

(Use Homework Problem 6.6 to generate more practice problems of this kind.)

Problem 7. Determine an orthogonal matrix P and a diagonal matrix D such that $A = PDP^T$.

- (a) If A is the 3×3 matrix for reflecting through the plane spanned by the vectors $\begin{bmatrix} 2 \\ 1 \\ 0 \end{bmatrix}, \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$.
- (b) If A is the 3×3 matrix for reflecting through the plane spanned by the vectors $\begin{bmatrix} 2 \\ 0 \\ 1 \end{bmatrix}, \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$.

(Use Homework Problem 8.2 to generate more practice problems of this kind.)

Problem 8.

- (a) The eigenvalues of a 5×5 matrix for orthogonally projecting onto a 3-dimensional subspace are .
What are the eigenspaces of that matrix?
- (b) Suppose A is the 3×3 matrix of a reflection through a plane (containing the origin).
Then $\det(A) = \text{$, and the eigenvalues of A are . What are the eigenspaces of A ?
- (c) Precisely state the spectral theorem.
- (d) If A is a reflection matrix, then $A^{-1} = \text{$.
- (e) If $A = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 4 \end{bmatrix}$, then $A^n = \text{$ and $e^{At} = \text{$.
- (f) If $N^4 = \mathbf{0}$, then $e^{Nt} = \text{$.