

EG $\begin{bmatrix} 4 & 1 \\ & 4 \end{bmatrix}$ diagonalizable? NO

$$\det \begin{pmatrix} 4-\lambda & 1 \\ 0 & 4-\lambda \end{pmatrix} = (4-\lambda)^2$$

\Rightarrow eigenvalues: $\lambda = 4, 4$

4-eigenspace = null $\begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix}$

only 1-dimensional

λ -Jordan block: $\begin{bmatrix} \lambda & 1 & & \\ & \lambda & \dots & \\ & & \ddots & 1 \\ & & & \lambda \end{bmatrix}$
eigenvalue λ
 m times repeated
 $m \times m$

λ -eigenspace only 1-dimensional

THM Every $n \times n$ matrix A can be written as $A = PJP^{-1}$ where

$$J = \begin{bmatrix} J_1 & & \\ & J_2 & \\ & & \ddots \end{bmatrix}$$

with each J_i being a Jordan block

unique up to ordering of J_i

J Jordan normal form of A