

Quiz #2

Please print your name:

Problem 1. Consider the region bounded by the curves $y = \sqrt{x}$, $y = 0$ and $x = 1$. Determine the area of this region.

Solution.

- First, you should make a sketch!
- Our region extends from $x = 0$ to $x = 1$ (no real need to compute intersections), so the area of our region is

$$\int_0^1 \sqrt{x} \, dx = \left[\frac{2}{3} x^{3/2} \right]_0^1 = \frac{2}{3}.$$

Problem 2. As in the previous problem, consider the region bounded by the curves $y = \sqrt{x}$, $y = 0$ and $x = 1$. Determine the volume of the solid generated by revolving this region about the x -axis.

Solution.

- Again, make a sketch first! (Or, in this case, refer to the earlier sketch.)
- Again, our region extends from $x = 0$ to $x = 1$, so the volume of our solid is

$$\int_0^1 \pi (\sqrt{x})^2 \, dx = \pi \int_0^1 x \, dx = \pi \left[\frac{1}{2} x^2 \right]_0^1 = \frac{\pi}{2}.$$

□