

Quiz #1

Please print your name:

Problem 1. Compute the following derivative:

$$\frac{d}{dx} \frac{1}{2x^3 - \cos(x)}$$

Solution. Using the chain rule, we find:

$$\frac{d}{dx} \frac{1}{2x^3 - \cos(x)} = -\frac{1}{(2x^3 - \cos(x))^2} \cdot (6x^2 + \sin(x))$$

Problem 2. Evaluate the following indefinite integral:

$$\int \sin^5(3t) \cos(3t) dt$$

Solution. We substitute $u = \sin(3t)$. Since

$$\frac{du}{dt} = 3\cos(3t),$$

we use $\cos(3t) dt = \frac{1}{3} du$ to get

$$\int \sin^5(3t) \cos(3t) dt = \frac{1}{3} \int u^5 du = \frac{1}{18} u^6 + C = \frac{1}{18} \sin^6(3t) + C.$$