

Quiz #5

Please print your name:

Problem 1. Expand $\frac{5x - 13}{(x - 3)(x - 2)}$ by partial fractions.

Solution. The numerator has degree less than the denominator, and the denominator is already factored for us.

Hence, $\frac{5x - 13}{(x - 3)(x - 2)} = \frac{A}{x - 3} + \frac{B}{x - 2}$ for some numbers A, B .

To find A, B , we clear denominators: $5x - 13 = (x - 2)A + (x - 3)B$.

Setting $x = 3$, we find $2 = A$. Setting $x = 2$, we find $-3 = -B$.

Hence, $\frac{5x - 13}{(x - 3)(x - 2)} = \frac{2}{x - 3} + \frac{3}{x - 2}$. □

Problem 2. Evaluate the integral $\int_1^2 x \ln(x) dx$.

Solution. We apply integration by parts, and use $\int f(x)g'(x)dx = f(x)g(x) - \int f'(x)g(x)dx$ with $f(x) = \ln(x)$ and $g'(x) = x$. With $g(x) = \frac{1}{2}x^2$, we then get

$$\int_1^2 x \ln(x) dx = \left[\frac{1}{2}x^2 \ln(x) \right]_1^2 - \int_1^2 \frac{1}{x} \cdot \frac{1}{2}x^2 dx = 2\ln(2) - \frac{1}{2} \int_1^2 x dx = 2\ln(2) - \frac{1}{2} \left[\frac{1}{2}x^2 \right]_1^2 = 2\ln(2) - \frac{3}{4}.$$
□