

# Quiz #6

Please print your name:

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**Problem 1. (4 points)** Compute the following derivatives.

[No need to show work.]

(a)  $\frac{d}{dx} \ln(x^3 + 7) =$

(b)  $\frac{d}{dx} [x^4 \tan^{-1}(x)] =$

**Solution.**

(a)  $\frac{d}{dx} \ln(x^3 + 7) = \frac{3x^2}{x^3 + 7}$

(b)  $\frac{d}{dx} [x^4 \tan^{-1}(x)] = 4x^3 \tan^{-1}(x) + \frac{x^4}{x^2 + 1}$

□

**Problem 2. (6 points)** Consider the curve  $x^3 + 2y^3 = xy$ .

[Show your work!]

(a) Using implicit differentiation, determine  $\frac{dy}{dx}$ .

(b) Determine the line tangent to the curve at the point  $(1, -1)$ .

**Solution.**

(a) Applying  $\frac{d}{dx}$  to both sides of  $x^3 + 2y^3 = xy$ , we obtain  $3x^2 + 6y^2 \frac{dy}{dx} = y + x \frac{dy}{dx}$ , so that  $\frac{dy}{dx} = \frac{y - 3x^2}{6y^2 - x}$ .

(b) The slope of the line tangent to the curve at  $(1, -1)$  is  $\left[ \frac{dy}{dx} \right]_{x=1, y=-1} = \left[ \frac{y - 3x^2}{6y^2 - x} \right]_{x=1, y=-1} = -\frac{4}{5}$ .

Hence, the tangent line has equation  $y + 1 = -\frac{4}{5}(x - 1)$ , which simplifies (optional) to  $y = -\frac{4}{5}x - \frac{1}{5}$ .

□